



Non Gaussian Long Memory Internet Traffic Statistical Modeling Application to Anomaly Detection.

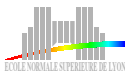
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Intimate 2006, July 6th-7th, Paris





Motivation and Goals: General Framework

Statistical Modeling

- Non Gaussian
- Short vs Long Range Dependence
- ↓ Detection

Regular Data

- Major Trace Repositories
- Self Collected
- a large variety of Traffic !

Anomaly Detection

- Detection Proc.
- Perf. Evaluation
- Need for a Database
- Classification

Data with Anomalies

- Documented Anomalies
- Reproducible, Controlled
- DDoS Attacks, Flash Crowds
- Low Level Intensities
- Real Network, Real Traffic



Outline

- 1 Modeling
 - Principles
 - Marginals
 - Covariances
 - Results, Estimation and Synthesis procedures
- 2 Detecting
 - Intuition and Principles
 - Anomaly DataBase
 - Statistical Performance
 - Classification
- 3 Conclusions and Perspectives
- 4 Appendix



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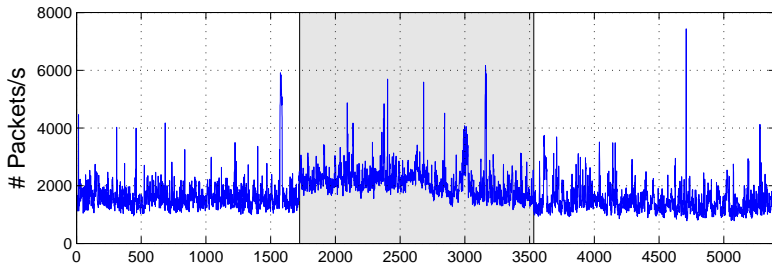


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Aggregated Time Series



- Aggregation level : Δ ,
- Packet Count,
- Byte Count,



Intuitions and Issues

- ① How should we choose a model ?
 - Based on significant data characteristics,
 - Parsimony,
 - Detection Goal in mind: parameters suited for detection.
- ② What should we model ?
 - Difficult: The full statistics (high order statistics) ?
 - Simple: Marginal Distributions ? Covariances ?
- ③ What Aggregation level should we choose ?
 - Small ? Large ? Compared to which scale ?
 - Depends on data ? on goals ?
- ④ Proposed Solutions
 - ① ⇒ Long Range vs Short range dependencies ?
Gaussian vs non Gaussian ?
 - ② ⇒ Trade-off: Marginals (1st stat order) and
covariances (2nd stat order) **jointly**
 - ③ ⇒ Modeling covariant with a change of aggregation level ?



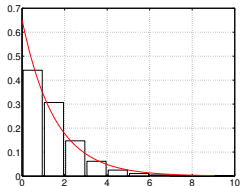
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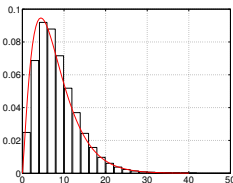


Marginals

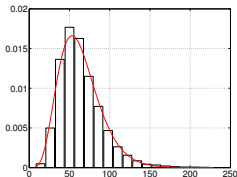
● Empirical PDFs LBL-TCP-3



$\Delta = 4\text{ms}$



$\Delta = 32\text{ms}$



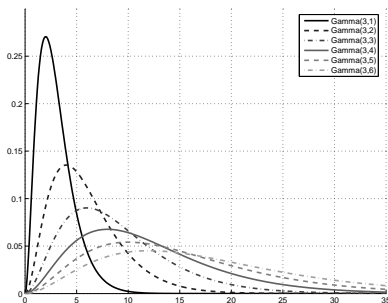
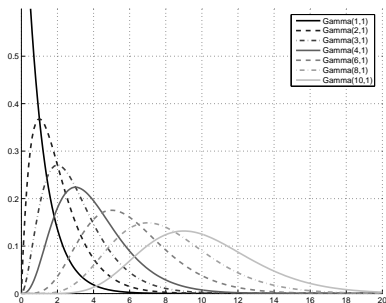
$\Delta = 256\text{ms}$

- Poisson ? Exponential ? Gaussian ?
- Aggregation level ?



Gamma Distributions

$$\Gamma_{\alpha,\beta}(x) = \frac{1}{\beta\Gamma(\alpha)} \left(\frac{x}{\beta}\right)^{\alpha-1} \exp\left(-\frac{x}{\beta}\right).$$

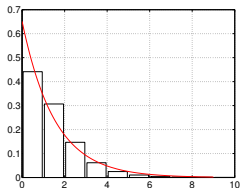


- Shape parameter α : From Gaussian to exponential, $1/\alpha \simeq$ distance from Gaussian,
- Scale parameter β : Multiplicative factor.

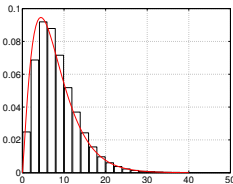


Gamma Fits

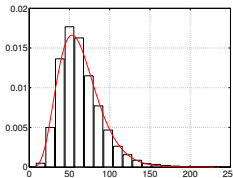
Empirical PDFs and Gamma Fits LBL-TCP-3



$\Delta = 4\text{ms}$



$\Delta = 32\text{ms}$



$\Delta = 256\text{ms}$

- Accurately Fits data for all aggregation levels Δ ,

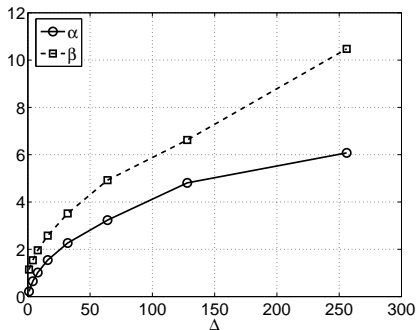
- Stability under addition :

$$X_1 : \Gamma_{\alpha_1, \beta}, X_2 : \Gamma_{\alpha_2, \beta}, (X_1, X_2) \text{ Indep.} \implies X_1 + X_2 : \Gamma_{\alpha_1 + \alpha_2, \beta},$$

- Aggregation : $X_{2\Delta}(k) = X_{\Delta}(k) + X_{\Delta}(k + 1)$.



Parameter Estimation: $\hat{\alpha}_\Delta, \hat{\beta}_\Delta$



- Stability under addition and Independence

$$\Rightarrow \begin{cases} \alpha(\Delta) = \alpha_0 \Delta \\ \beta(\Delta) = \beta_0 \end{cases}$$

- $\hat{\alpha}_\Delta, \hat{\beta}_\Delta$ accommodate correlations !



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Covariance : the wavelet point of view

- X_Δ stationary stochastic process, with spectrum $f_{X_\Delta}(\nu)$,
- Wavelet Coefficients: $d_X(j, k)$,

► WaveletTransform

- Wavelet Spectrum: $S(j) = \frac{1}{n_j} \sum_{k=1}^{n_j} |d_{X_\Delta}(j, k)|^2$,

$$\mathbb{E}S(j) = \int f_X(\nu) 2^j |\Psi_0(2^j \nu)|^2 d\nu \simeq \hat{f}_X(\nu = 2^{-j} \nu_0).$$

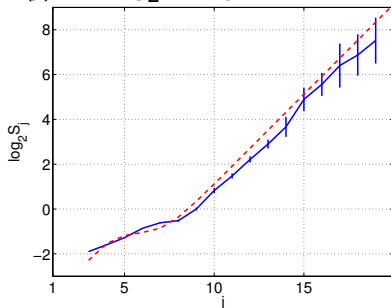
- Log-scale Diagram: $\log_2 S_2(j)$ vs. $\log_2 2^j = j$.



Both Short and Long Range Dependencies

- **Log-scale Diagram:** $\log_2 S_2(j)$ vs. $\log_2 2^j = j$.

X_Δ , LBL-TCP-3, $\Delta = 1\text{ms}$



- Power law at coarse scales (low frequencies):
 \Rightarrow Long range dependence,
- Short dependence at fine scales (low frequencies),
- \Rightarrow Use a FARIMA(P, d, Q) covariance form.



FARIMA(P, d, Q) covariance

farima = fractionally Integrated ARMA.

- 1 fractional integration with parameter d ,
- 2 short-range correlations as an ARMA(1,1) \rightarrow params. θ, ϕ .

$$f_{X_{\Delta}}(\nu) = \sigma_{\epsilon}^2 \left| 1 - e^{-i2\pi\nu} \right|^{-2d} \frac{|1 - \theta e^{-i2\pi\nu}|^2}{|1 - \phi e^{-i2\pi\nu}|^2},$$

- d controls Long Range Dep., with $\gamma = 2d$,

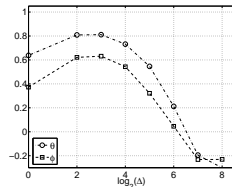
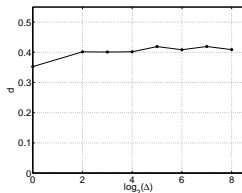
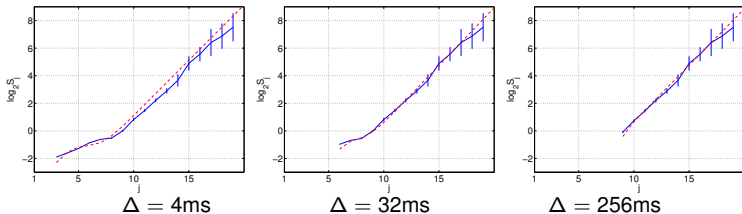
► LRD

- P, Q control Short Range Dep.



Empirical LDs and FARIMA(P,d,Q) Fits

LBL-TCP-3



- Accurately Fits data for all aggregation levels Δ ,
- LRD is persistent, SRD are cancelled out.



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Non Gaussian Long Range Dependent Models

- Jointly 1st and 2nd order statistics,
- Parsimony,
- Covariance with respect to the Aggregation level Δ ,
[▶ ShowResults](#)
- For various data, various traffics, various links, various networks,
[▶ TableData](#)
- Suboptimal but robust and low cost parameter estimation procedures,
- Numerical synthesis procedures (with A. Scherrer, LIP6, ENS Lyon),
[▶ NumericalSynthesis](#)
- Detection ?



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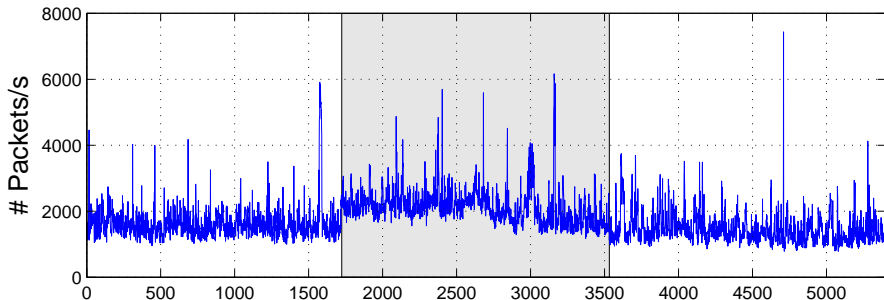


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Aggregated Time Series

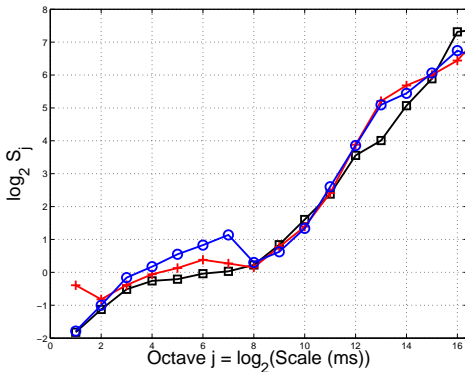


- IPerf, UDP Flooding.



DDoS Attack (UDP Flooding)

LogScale Diagrams

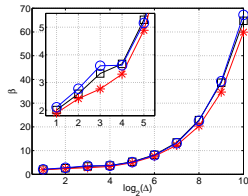
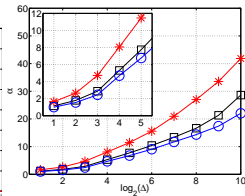
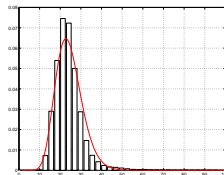
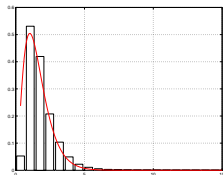


- Black: before, Red: during, blue: After Attack.
- LRD not caused by nor altered by DDoS Attacks.



DDoS Attack (UDP Flooding)

Gamma Fits (during attack)



- Black: before, Red: during, blue: After Attack,
- Model fits data with anomaly equally satisfactorily,
- Goes faster to Gaussian \rightarrow DDoS changes the SRD,
- Multiresolution nature (multi Δ) of the model.



Principles

- Choose a Reference time windows,
- Split data into sliding time windows of length T ,
- For each time window l :
 - Aggregate data at levels $\Delta = 2^j, j = 1, \dots, J$
 - Estimate the chosen statistics: $\hat{\alpha}_\Delta(l), \hat{\beta}_\Delta(l)$
 - Compute a distance between l and R

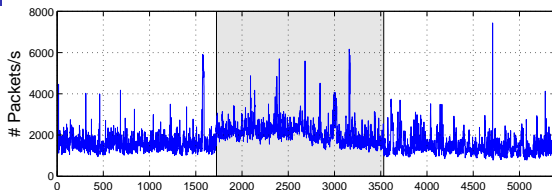
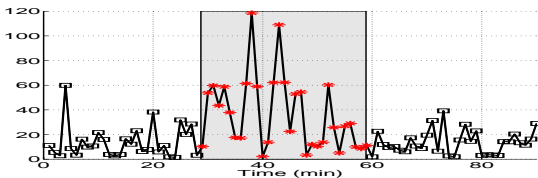
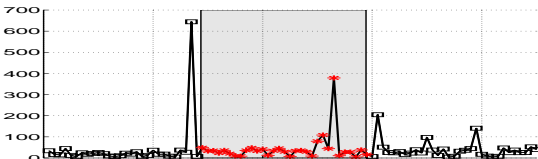
$$D_\alpha(l) = \frac{1}{J} \sum_{j=1}^J (\hat{\alpha}_{2^j}(l) - \hat{\alpha}_{2^j}(ref))^2, \quad (1)$$

$$D_\beta(l) = \frac{1}{J} \sum_{j=1}^J (\hat{\beta}_{2^j}(l) - \hat{\beta}_{2^j}(ref))^2. \quad (2)$$

- Choose a threshold λ to decide when the distance is *too large*, $D_\alpha(l) \geq \lambda$.

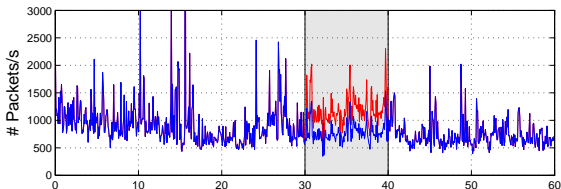
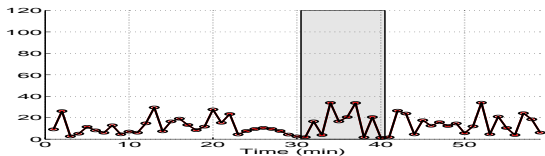
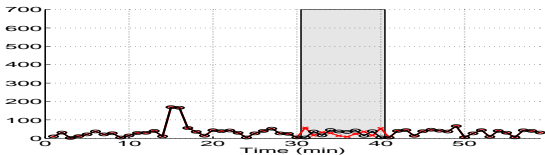


Example 1 : DDoS Attack


 $D_{\alpha}(I)$

 $D_{\beta}(I)$




Example 2 : Artificial Multiplicative Traffic Increase


 $D_\alpha(I)$

 $D_\beta(I)$




Statistical performance ?

- Receiver Operating Curves:
How many false positive given the false negative ?
- $P_D = f(P_F)$ or $P_D = f(\lambda)$, $P_F = f(\lambda)$,
- \Rightarrow Need for a documented anomaly dataBase !!!

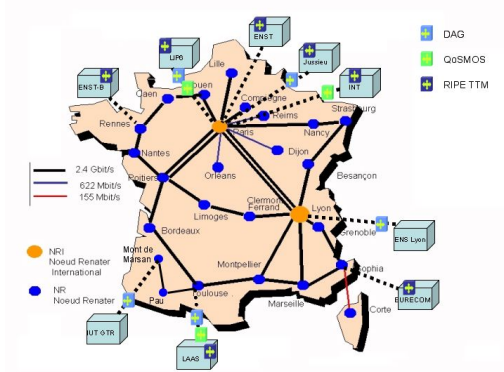


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Anomaly DataBase: Topology



- METROSEC partners (all over France),
- Lyon, Nice, Paris, Mont-de-Marsan, Coimbra \Rightarrow Toulouse,
- RENATER network,



Anomaly DataBase: Typology

- UDP Flooding, IPperf, Trinoo.
- Increase Link/Routeur load \Rightarrow Decrease QoS.
- Emulate a small Leave of a huge Botnet Tree:
 - Moraly* close to the source,
 - Low Intensity Level Attack,
 - Before Effective Impact on QoS,
 - \Rightarrow Difficult to detect.
- In progress: TFN2K : SYN, ICMP flooding, Smurf, Targa3.



Anomaly DataBase - DDoS Attacks -2004 - 2006

| Id | t_i | $T(s)$ | t_a | $T_A(s)$ | D | V | $I(%)$ |
|----------------------------|-------|--------|-------|----------|------|------|--------|
| DDoS performed with Iperf | | | | | | | |
| R | 17:30 | 60000 | 20:00 | 20000 | 0.5 | 60 | 33.82 |
| I | 09:54 | 5400 | 10:22 | 1800 | 0.25 | 1500 | 17.06 |
| II | 14:00 | 5400 | 14:29 | 1800 | 0.5 | 1500 | 14.83 |
| III | 16:00 | 5400 | 16:29 | 1800 | 0.75 | 1500 | 21.51 |
| IV | 10:09 | 5400 | 10:16 | 2500 | 1.0 | 1500 | 33.29 |
| V | 10:00 | 5400 | 10:28 | 1800 | 1.25 | 1500 | 39.26 |
| A | 14:00 | 5400 | 14:28 | 1800 | 1 | 1000 | 34.94 |
| B | 16:00 | 5400 | 16:28 | 1800 | 1 | 500 | 40.39 |
| C | 10:03 | 5400 | 10:28 | 1800 | 1 | 250 | 36.93 |
| DDoS performed with Trinoo | | | | | | | |
| tM | 18:21 | 5400 | 18:58 | 601 | 0.1 | 300 | 4.64 |
| tN | 18:22 | 3600 | 18:51 | 601 | 0.1 | 300 | 15.18 |
| tT | 18:22 | 3600 | 18:51 | 601 | 8 | 300 | 82.85 |



Anomaly DataBase - Flash Crowds - 2005 - 2006

| Id | t_i | $T(s)$ | t_a | $T_A(s)$ | D | V | $I(\%)$ |
|-----------------------|-------|--------|-------|----------|-----|-----|---------|
| FC performed by human | | | | | | | |
| FC-1 | 13:45 | 7200 | 14:30 | 1800 | — | — | 31.27 |
| FC-2 | 15:00 | 7200 | 15:45 | 1800 | — | — | 18.35 |



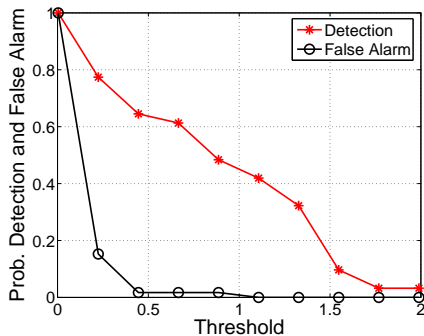
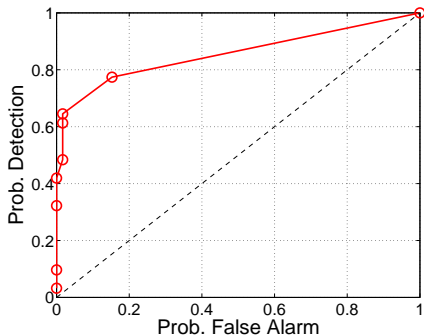
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Stat. Perf.: Receiver Operating Curves

- How many false positive given the false negative ?
- $P_D = f(P_F)$ or $P_D = f(\lambda)$, $P_F = f(\lambda)$,





Stat. Perf.: Detection Probability

| Type of Anomaly | performed with | Id | Intens. (%) | P_D | |
|-----------------|----------------|-----|-------------|--------------|--------------|
| | | | | $P_F = 10\%$ | $P_F = 20\%$ |
| DDoS | Iperf | R | 33.82 | 91 | 93 |
| DDoS | Iperf | I | 17.06 | 51 | 64 |
| DDoS | Iperf | II | 14.83 | 48 | 54 |
| DDoS | Iperf | III | 21.51 | 48 | 58 |
| DDoS | Iperf | IV | 33.29 | 33 | 50 |
| DDoS | Iperf | V | 39.26 | 18 | 40 |
| DDoS | Iperf | A | 34.94 | 21 | 50 |
| DDoS | Iperf | B | 40.39 | 81 | 87 |
| DDoS | Iperf | C | 36.93 | 52 | 58 |
| DDoS | Trinoo | tM | 4.64 | 27 | 50 |
| DDoS | Trinoo | tN | 15.18 | 54 | 54 |
| DDoS | Trinoo | tT | 82.85 | 82 | 82 |



Stat. Perf.: use of other distances/other thresholds

- Kullback divergence :

$$KD(p_1, p_2) = \int (p_1 - p_2)(\ln p_1 - \ln p_2) dx$$

- 1D : $K_{\Delta}^{(1D)}(I) = KD(p_{\Delta, I}, p_{\Delta, Ref})$
- 2D : $K_{\Delta, \Delta'}^{(2D)}(I) = KD(p_{\Delta, \Delta', I}, p_{\Delta, \Delta', Ref})$
- Multiple consecutive threshold bypasses.

| | D_{α} | $K_{24}^{(1D)}$ | $K_{27}^{(1D)}$ | $K_{24, 27}^{(2D)}$ |
|------------|--------------|-----------------|-----------------|---------------------|
| I | 51 : 64 | 25 : 64 | 35 : 67 | 25 : 51 |
| II | 48 : 54 | 35 : 58 | 35 : 61 | 35 : 61 |
| III | 48 : 58 | 74 : 93 | 70 : 83 | 87 : 93 |
| IV | 33 : 50 | 56 : 67 | 56 : 69 | 34 : 66 |
| V | 18 : 40 | 87 : 96 | 34 : 93 | 90 : 96 |
| A | 21 : 50 | 50 : 78 | 37 : 59 | 53 : 81 |
| B | 81 : 87 | 78 : 78 | 09 : 33 | 78 : 81 |
| C | 52 : 58 | 91 : 91 | 91 : 91 | 91 : 91 |
| X | 93 : 96 | 93 : 93 | 93 : 93 | 93 : 93 |
| tM | 27 : 55 | 36 : 91 | 36 : 91 | 45 : 91 |
| tN | 54 : 54 | 73 : 91 | 91 : 91 | 55 : 73 |
| tT | 82 : 82 | 100 : 100 | 100 : 100 | 100 : 100 |

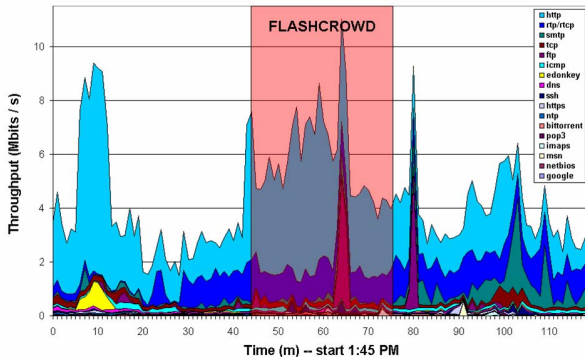


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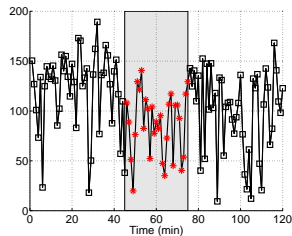
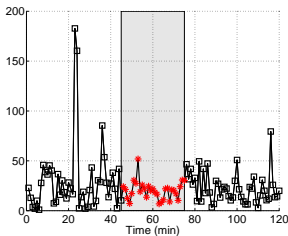
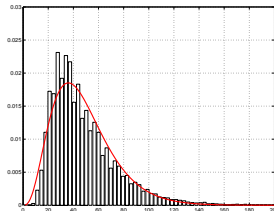
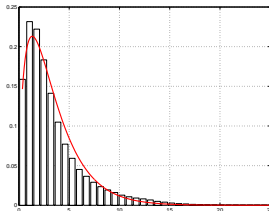
Flash Crowd



- Operated by Humans.



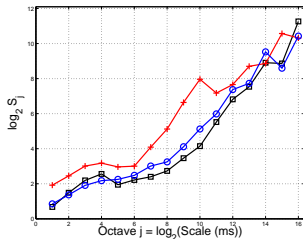
Flash Crowd and Gamma Fits



- Model fits data with anomaly equally satisfactorily
- But Flash Crowd does not change the SRD.



Flash Crowd and LogScale Diagrams



- LRD not caused by nor altered by Flash Crowd,
- SRD not altered by Flash Crowd,
- Medium Range Dependencies altered,
- Distances on LDs \Rightarrow Detection and Classification.



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Conclusions

- Conclusions:
 - Non Gaussian/ Gaussian,
 - Short vs Long range Dependence,
 - Versatile and parsimonious modeling,
 - Detection/Classification oriented,
 - Synthetic traffic generation,
 - Performance Evaluation methodology,



Perspectives

- Perspectives:
 - Comparison against other tools, IDS ?
 - A richer DataBase ?
 - QoS Impact ?
 - Adaptive Reference ?
 - Detection far from sources ?
 - Multivariate data ? Multi-Point Analysis ?
 - Robustness: Split traffic into OD pairs ?
 - Partial sampling ?
 - Joint Topology and Time Series Detection ?



Further Information

- Mails:

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`owe@laas.fr`

- URL (reprints and preprints):

`perso.ens-lyon.fr/patrice.abry`

`ens-lyon.fr/PHYSIQUE`

`www2.laas.fr/METROSEC/`



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Long Range Dependence

Definition of Long Range Dependence

Covariance is a non-summable power-law \rightarrow spectrum $f_{X_\Delta}(\nu)$:

$$f_{X_\Delta}(\nu) \sim C|\nu|^{-\gamma}, |\nu| \rightarrow 0, \text{ with } 0 < \gamma < 1.$$

Long Range Dependence and Wavelets

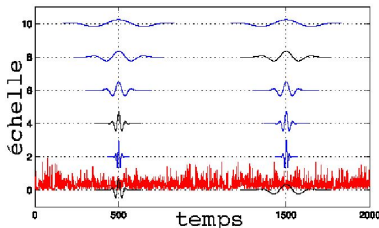
$$\mathbb{E}S(j) = \int f_X(\nu) 2^j |\Psi_0(2^j \nu)|^2 d\nu \simeq \hat{f}_X(\nu = 2^{-j} \nu_0).$$

$$\text{LRD} \implies \mathbb{E}S(j) \sim C 2^{j(\gamma-1)}, 2^j \rightarrow +\infty.$$

Wavelet Transform

- Let ψ_0 denote an elementary mother wavelet,
- Shifted and dilated templates of ψ_0 :

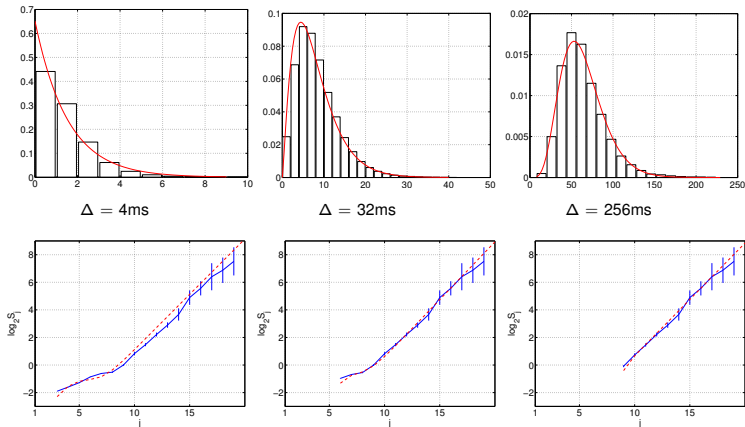
$$\psi_{j,k}(t) = 2^{-j/2} \psi_0(2^{-j}t - k),$$
- Wavelet Coefficients: $d_{X_\Delta}(j, k) = \langle \psi_{j,k}, X_\Delta \rangle$.





Model (8/) : Jointly 1st and 2nd order statistics

1st order stat. Marginals fitted by Γ -laws.



2nd order stat. Covariance fitted by a FARIMA(P, d, Q)

[◀ Back](#)



TableData

- A variety of traces from major repositories were tested.
- Data collected on the french Renater network, by the METROSEC project (Metrology for Security on the Internet).

| Data | Date(Start Time) | T (s) | Network(Link) | # Pkts | IAT (ms) | Repository |
|-----------|-------------------|-------|----------------|--------|----------|---------------------------------|
| PAUG | 1989-08-29(11:25) | 2620 | LAN(10BaseT) | 1 | 2.6 | ita.ee.lbl.gov/index.html |
| LBL-TCP-3 | 1994-01-20(14:10) | 7200 | WAN(10BaseT) | 1.7 | 4 | ita.ee.lbl.gov/index.html |
| AUCK-IV | 2001-04-02(13:00) | 10800 | WAN(OC3) | 9 | 1.2 | wand.cs.waikato.ac.nz/wand/wits |
| CAIDA | 2002-08-14(10:00) | 600 | Backbone(OC48) | 65 | 0.01 | www.caida.org/ |
| UNC | 2003-04-06(16:00) | 3600 | WAN(10BaseT) | 4.6 | 0.8 | www-dirt.cs.unc.edu/ts/ |
| MTS-ref1 | 2004-12-09(18:30) | 5000 | LAN(10BaseT) | 3.9 | 1.5 | www.laas.fr/METROSEC/ |
| MTS-ref2 | 2004-12-10(02:00) | 9000 | LAN(10BaseT) | 2.1 | 4.3 | www.laas.fr/METROSEC/ |
| MTS-ref3 | 2006-03-20(11:00) | 3600 | LAN(10BaseT) | 2.8 | 3.7 | www.laas.fr/METROSEC/ |
| MTS-ref4 | 2004-12-21(15:00) | 3600 | LAN(10BaseT) | 2.9 | 3.9 | www.laas.fr/METROSEC/ |

◀ Back



Synthesis of a Γ -farima process

Procedure.

- **Mapping – 1st order stat.:** if $Y_j(k)$ is a Gaussian r.v. with variance $\beta/2$, then

$$X(k) = \sum_{j=1}^{2\alpha} Y_j(k)^2 \quad (3)$$

is a $\Gamma_{\alpha,\beta}$ r.v.

- **Mapping – 2nd order stat.:** as a consequence,

$$\gamma_Y(k) = \sqrt{\gamma_X(k)/4\alpha}. \quad (4)$$

- **Procedure:** generate 2α Gaussian processes with covariance γ_Y derived with (2) from the farima covariance, then obtain X from (1).

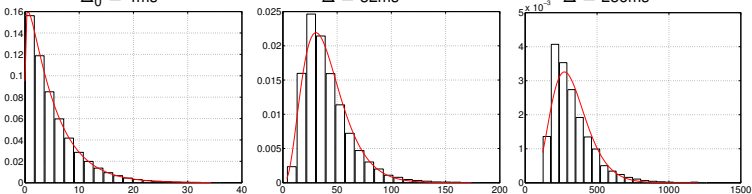
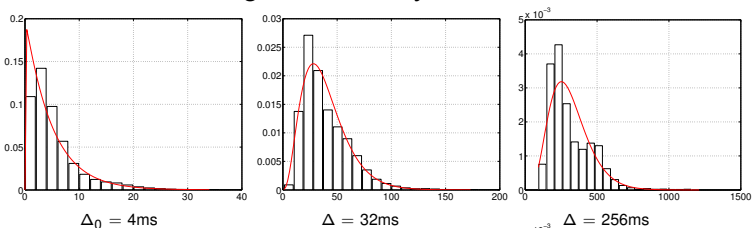


Empirical PDF and $\Gamma_{\alpha,\beta}$ models

Metrosec-fc1

1st order stat. Marginals fitted by Γ -laws.

Data



Model

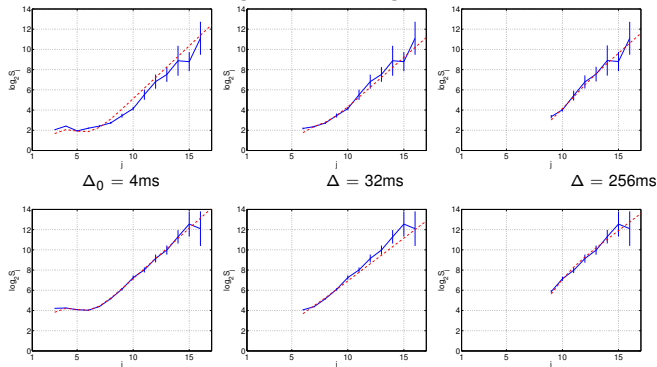


Empirical PDF and $\Gamma_{\alpha,\beta}$ models

Metrosec-fc1

2nd order stat. Log-Scale Diagram

Data



Model

◀ Back